

Mapping of Applications to Platforms

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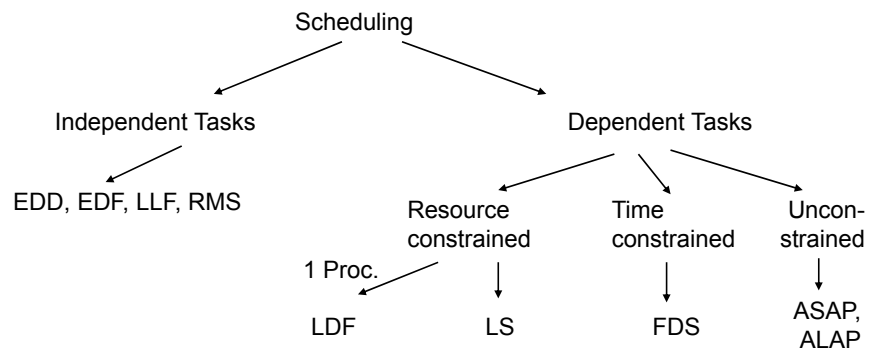


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(2010年 12月 10日)
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Classification of Scheduling Problems



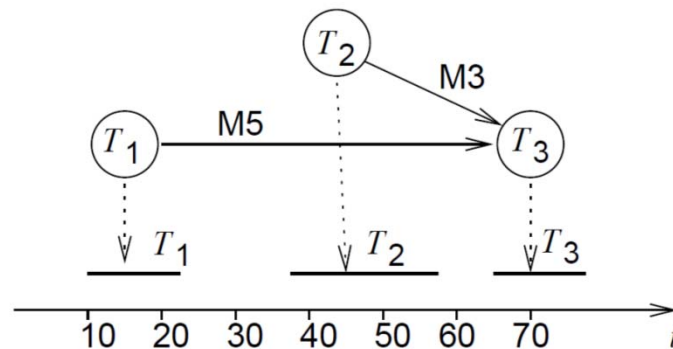
Overview

Scheduling of aperiodic tasks with real-time constraints:
Table with some known algorithms:

	Equal arrival times; non-preemptive	Arbitrary arrival times; preemptive
Independent tasks	EDD (Jackson)	EDF (Horn)
Dependent tasks	LDF (Lawler), ASAP, ALAP, LS, FDS	EDF* (Chetto)

Scheduling with precedence constraints

Task graph and possible schedule:

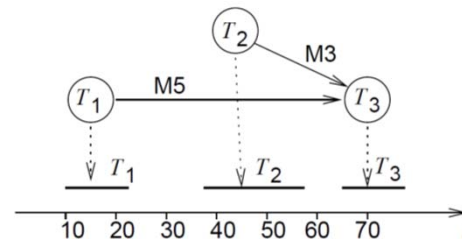


Simultaneous Arrival Times: The Latest Deadline First (LDF) Algorithm

LDF [Lawler, 1973]: reads the task graph and **among the tasks with no successors inserts the one with the latest deadline** into a queue. It then repeats this process, putting tasks whose successor have all been selected into the queue.

At run-time, the tasks are executed in the **opposite** of the generated total order.

LDF is non-preemptive and is optimal for mono-processors.



If no local deadlines exist, LDF performs just a topological sort.

Asynchronous Arrival Times: Modified EDF Algorithm

This case can be handled with a modified EDF algorithm. The key idea is to transform the problem from a given set of dependent tasks into a set of independent tasks with different timing parameters [Chetto90].

This algorithm is optimal for mono-processor systems.

If preemption is not allowed, the heuristic algorithm developed by Stankovic and Ramamritham can be used.

Static Scheduling with Dependencies: Scheduling in High-Level Synthesis

- HLS-based scheduling
 - ASAP
 - ALAP
 - List scheduling (LS)
 - *Force-directed scheduling (FDS)*

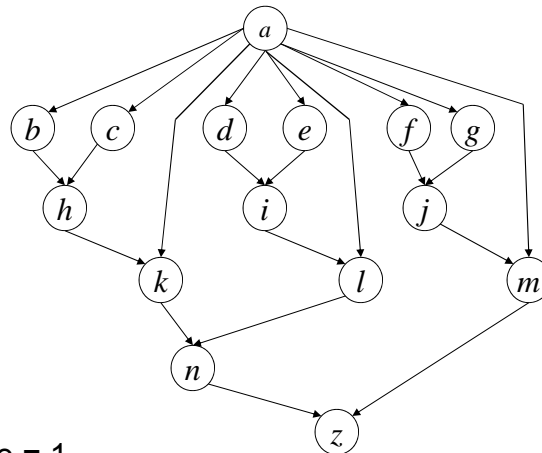
Dependent tasks

The problem of deciding whether or not a schedule exists for a set of dependent tasks and a given deadline is NP-complete in general [Garey/Johnson].

Strategies:

1. Add resources, so that scheduling becomes easier
2. Split problem into static and dynamic part so that only a minimum of decisions need to be taken at run-time.
- ➡ 3. Use scheduling algorithms from high-level synthesis

Task graph



Assumption:
execution time = 1
for all tasks

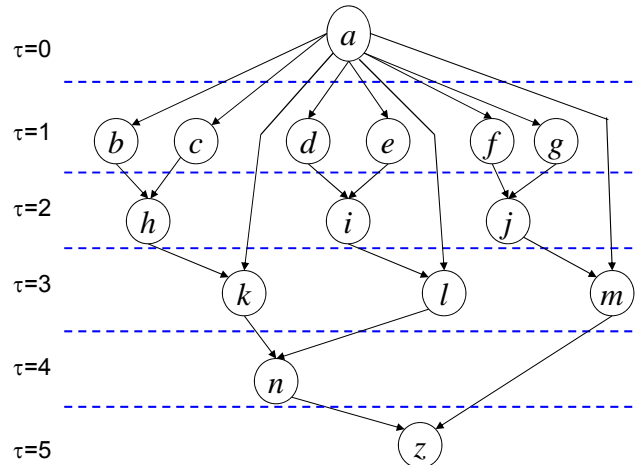
As soon as possible (ASAP) scheduling

ASAP: All tasks are scheduled as early as possible

Loop over (integer) time steps:

- Compute the set of unscheduled tasks for which all predecessors have finished their computation
- Schedule these tasks to start at the current time step.

As soon as possible (ASAP) scheduling: Example



As-late-as-possible (ALAP) scheduling

ALAP: All tasks are scheduled as late as possible

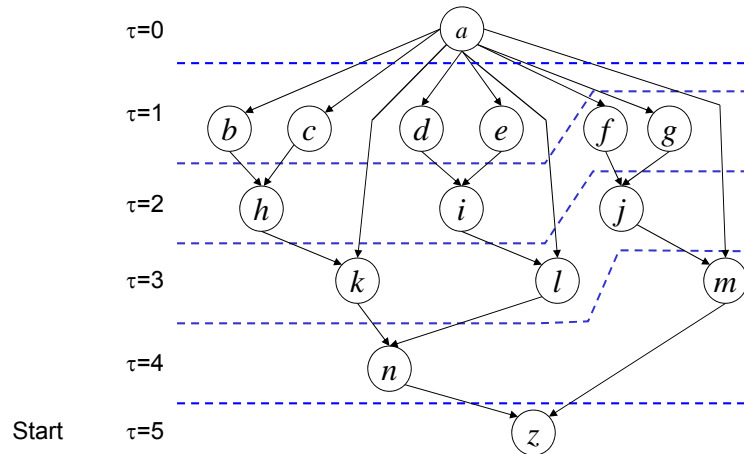
Start at last time step*:



Schedule tasks with no successors and tasks for which all successors have already been scheduled.

* Generate a list, starting at its end

As-late-as-possible (ALAP) scheduling: Example



(Resource constrained) List Scheduling

List scheduling: extension of ALAP/ASAP method

Preparation:

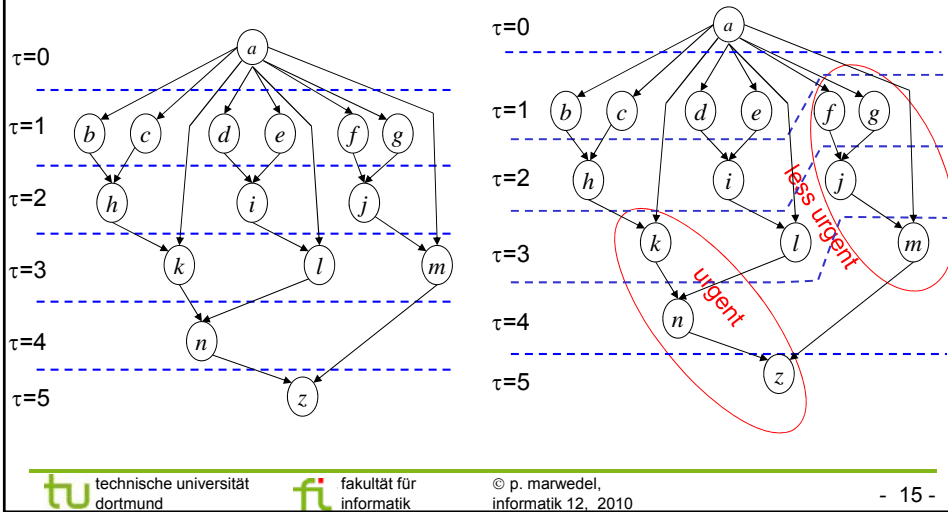
- Topological sort of task graph $G=(V,E)$
- Computation of priority of each task:

Possible priorities u :

- Number of successors
- Longest path
- **Mobility** = τ (ALAP schedule) - τ (ASAP schedule)

Mobility as a priority function

Mobility is not very precise



List Scheduling Algorithm

List($G(V,E), B, u$) {

$i := 0$;

repeat {

 Compute set of candidate tasks A_i ;

 Compute set of not terminated tasks G_i ;

 Select $S_i \subseteq A_i$ of maximum priority r such that $|S_i| + |G_i| \leq B$ (*resource constraint*)

 foreach ($v_j \in S_i$): $\tau(v_j) := i$; (*set start time*)

$i := i + 1$;

}

until (all nodes are scheduled);

return (τ);

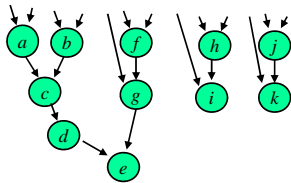
}

} may be repeated for different task/processor classes

Complexity: $O(|V|)$

Example

Assuming $B = 2$, unit execution time and u : path length



$$\begin{aligned} u(a) &= u(b) = 4 \\ u(c) &= u(f) = 3 \\ u(d) &= u(g) = u(h) = u(j) = 2 \\ u(e) &= u(i) = u(k) = 1 \\ \forall i : G_i &= 0 \end{aligned}$$

Modified example
based on J. Teich

