

EECS 10: COMP METHODS IN ECE

Discussion 8

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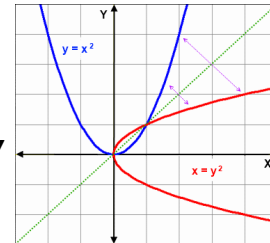
Assignment Discussion

- Assignment 4
 - A menu-driven calculator for floating point numbers
 - Addition, Subtraction, Square root, ...
1. Add a floating point number to the current result;
 2. Subtract a floating point number from the current result;
 3. Multiply the current result by a floating point number;
 4. Divide the current result by a floating point number;
 5. Take the absolute value of the current result;
 6. Get the approximate square root of the current result;
 7. Get the sine of the current result;
 8. Get the cosine of the current result;
 9. Get the tangent of the current result;
 10. Get the approximate Nth root of the current result;
 11. Quit.

Today

Approximate Square Root

- Binary search for the square root of a floating point number.
 - Suppose N is a non-negative number, and s is its square root.
1. $L = 0, R = \max(1, N)$
 2. $L * L \leq N == S * S \leq R * R$
 3. $M = L + (R - L) / 2$
 4. if $\text{Abs}(M * M - N) < 0.00001,$
return M
 5. if $M * M > N, R = M, \text{ goto } 3$
 6. if $M * M < N, L = M, \text{ goto } 3$



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Approximate Square Root

- Example 1: $N = 9, S = 3$
 1. $L = 0, R = 9, M = 4.5, M * M > N$
 2. $L = 0, R = 4.5, M = 2.25, M * M < N$
 3. $L = 2.25, R = 4.5, M = 3.375, M * M > N$
 4. $L = 2.25, R = 3.375, M = 2.8125, M * M < N$
 - ...
 21. $M = 3.000001$

Iteration 1: the square root of 9.000000 is approximately 4.500000
 Iteration 2: the square root of 9.000000 is approximately 2.250000
 Iteration 3: the square root of 9.000000 is approximately 3.375000
 Iteration 4: the square root of 9.000000 is approximately 2.812500
 ...
 Iteration 21: the square root of 9.000000 is approximately 3.000001

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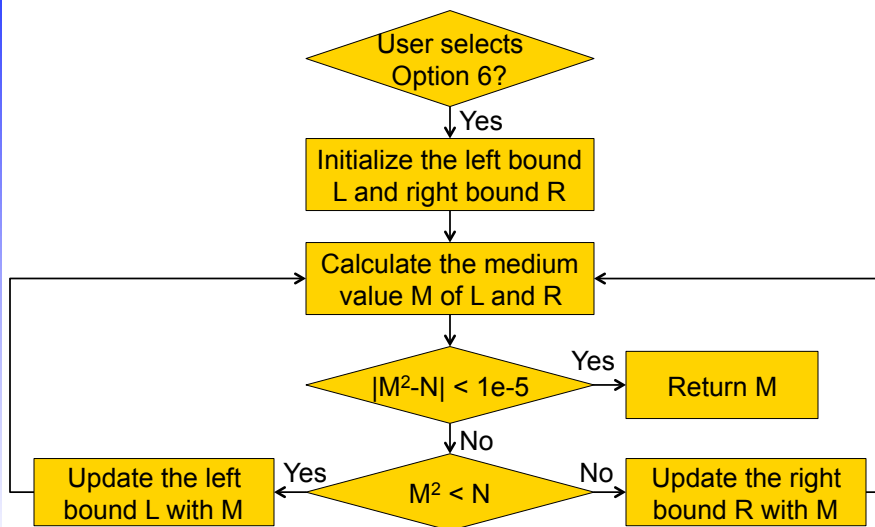
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Approximate Square Root

- Example 2: $N = 0.81$, $S = 0.9$
 1. $L = 0$, $R = 1$, $M = 0.5$, $M * M < N$
 2. $L = 0.5$, $R = 1$, $M = 0.75$, $M * M < N$
 3. $L = 0.75$, $R = 1$, $M = 0.875$, $M * M < N$
 4. $L = 0.875$, $R = 1$, $M = 0.9375$, $M * M > N$
 - ...
 17. $M = 0.900002$

Iteration 1: the square root of 0.810000 is approximately 0.500000
 Iteration 2: the square root of 0.810000 is approximately 0.750000
 Iteration 3: the square root of 0.810000 is approximately 0.875000
 Iteration 4: the square root of 0.810000 is approximately 0.937500
 ...
 Iteration 17: the square root of 0.810000 is approximately 0.900002

Control Flow



Bonus: Approximate Nth Root

- Binary search for the Nth root of a floating point number
 - Suppose N is a non-negative number, and s is its Nth root.
 - 1. $L = 0, R = \max(1, N)$
 - 2. $L * L * \dots * L \leq N == S * S * \dots * S \leq R * R * \dots * R$
 - 3. $M = L + (R - L) / 2$
 - 4. $M * M * \dots * M ? N$
- Prompt the user to enter an integer number
Please input the value of integer n(n>0):

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Sin, Cos and Tan

- Reuse the formula in Assignment 2 to calculate these values

$$\sin(x) = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{(2n+1)!} = x - \frac{x^3}{6} + \frac{x^5}{120} - \frac{x^7}{5040} + \frac{x^9}{362880} + \dots$$

$$\cos(x) = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!} = 1 - \frac{x^2}{2} + \frac{x^4}{24} - \frac{x^6}{720} + \frac{x^8}{40320} + \dots$$

$$\tan(x) = x + \frac{x^3}{3} + \frac{2}{15}x^5 + \frac{17}{315}x^7 + \frac{62}{2835}x^9 + \frac{1382}{155925}x^{11} + \frac{21844}{6081075}x^{13} + \dots$$

- Still use `double` as the data type

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Program Requirements

- Define a separate function for each operation


```
double ApproximateRoot2(double op1);
double ApproximateSin(double op1);
double ApproximateCos(double op1);
double ApproximateTan(double op1);
double ApproximateRootN(double op1, unsigned
int N);
```
- Do not use the C standard math library!
- Error handling
 - Print out an error message when the operand is invalid.
 - Prompt the user until a proper operand is entered.

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Assignment Discussion

- Error handling
 - “ERROR: Input out of the range!” for the tan function
 - “ERROR: Square root of a negative number!” for the square root function
 - “ERROR: Nth root of a negative number!” and “ERROR: Invalid integer N!” for the Nth root function
 - ...

```
Please enter a selection: 10
-----
Please input the value of integer n(n>0): 0
ERROR: Invalid integer N!
Please input the value of integer n(n>0):
```
- Verify your program with steps on Page 6
- Name your files as **calculator.c**, **calculator.txt** and **calculator.script**

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